Quantum Interference between the Third and Fourth Exciton States in Semiconducting Carbon Nanotubes Using Resonance Raman Spectroscopy

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We exploit an energy level crossover effect [Haroz et al., Phys. Rev. B 77, 125405 (2008)] to probe quantum interference in the resonance Raman response from carbon nanotube samples highly enriched in the single semiconducting chiralities of (8,6), (9,4), and (10,5). UV Raman excitation profiles of G-band spectra reveal unambiguous signatures of interference between the third and fourth excitonic states (E₃ and E₄). Both constructive and destructive responses are observed and lead to anomalous intensity ratios in the LO and TO modes. Especially large anomalies for the (10,5) structure result from nearly identical energies found for the two Eᵢ excitations. The interference patterns demonstrate that the sign of the exciton–phonon coupling matrix elements changes for the LO mode between the two electronic states, and remains the same for the TO mode. Significant non-Condon contributions to the Raman response are also found.

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Single-wall carbon nanotubes (SWCNTs) serve as model 1D systems for studying distinctive electronic and optical phenomena, including ballistic transport, the Kohn anomaly, the Aharonov-Bohm effect, and exciton physics [1]. Their narrow, intense, excitonic transitions also make them nearly ideal for exploring another important optical behavior: quantum interference in the Raman response from closely spaced electronic states [2,3], an important subset of interference as a more general wave concept for any coherent interaction. Raman interference in molecular and solid-state systems has been studied extensively, and has been used to reveal forbidden transitions and hidden nonresonant behavior [4–7]. Often, however, broad spectra and measurement of low-frequency phonons prevent resolution of the relevant interfering resonances. Furthermore, spacing of interfering states is not readily tuned, limiting detailed study of the effect. SWCNTs, however, provide both structurally tunable transition energies [1] and access to high frequency modes for study. Theoretical recognition of the potential for interference effects in SWCNTs [8] has provided a basis for detailed analysis and attempts at direct measurement of interference via Raman excitation profiling on single tubes [9]. However, these results likely suffer from uncertainty in assignment of structural (n,m) indices and samples that probably occur as small bundles. Additionally, the possibility of interference between closely spaced upper and lower branches of metallic SWCNTs [10] has been inferred from indirect measurements [11]. Modeling of potential interference effects over multiple SWCNT structures has also been presented [12].

Interference in SWCNTs represents the phenomenon for very distinct points in the graphene k space. Interference phenomena in graphene itself has only recently been demonstrated via blocking of Raman G-mode interference pathways by electrostatic gating [13].

In semiconducting SWCNTs, interference becomes a possibility with resonance excitation into the third and fourth excitonic levels (E₃ and E₄). For small-diameter mod 2 structures (n·m mod 3 = 2), the energies of these two states can approach closely and even cross over for certain chiralities [14,15], potentially leading to pronounced Raman interference effects. A clear demonstration of interference at the ensemble level requires resonance Raman excitation profiles (REPs) obtained from samples that are highly enriched in single chiralities, in order to avoid overlapping spectral response from other species. By acquiring REPs of the E₃ and E₄ transitions for the (8,6), (9,4), and (10,5) chiralities, we show here unambiguous evidence of quantum interference in the Raman response of the LO and TO G-band modes, which can lead to anomalous LO and TO intensity ratios. Furthermore, the relative signs of the LO matrix elements are found to reverse for the two transitions, while they remain the same for the TO mode. For the chiralities studied, systematic variation of Eᵢ energies with tube structure allows us to observe a range of interference effects as a function of energy separation between the interfering transitions. Analysis of the REPs also reveals evidence that recently discovered asymmetric responses
arising from non-Condon activity [16] are significant in these transitions as well.

Resonance Raman spectroscopy is performed on separate samples that have been highly enriched (>95%) in the (8,6), (9,4), and (10,5) mod 2 semiconductor chiralities via the previously reported DNA-based ion-exchange chromatography [17]. Following separation, SWCNTs in each sample are dialyzed into deoxycholate. Absorption spectra covering the second, third, and fourth excitonic transitions are shown in Fig. 1(a). For (8,6) and (9,4), the $E_{33}$ and $E_{44}$ transitions are well resolved. We note that the energy ordering of the third and fourth transitions is reversed for (9,4) [15]. For (10,5) the two transitions overlap and are not resolved. Extended tight binding calculations predict the (10,5) $E_{33}$ and $E_{44}$ to be within 50 meV of each other [18].

The intensity of the (10,5) $E_{33}/E_{44}$ feature also bears that of the $E_{22}$ [in comparison to the roughly half intensity shown for the individual (8,6) and (9,4) features], further suggesting the two transitions are nearly equal in energy for (10,5). For all three chiralities, energy separations of $E_{33}$ and $E_{44}$ are on the order of, or less than, the G-band energy (~197 meV), suggesting significant Raman interference effects might be expected.

Radial breathing mode (RBM) and G-band Raman spectra were obtained with 20 mW of excitation ranging from 2.92 to 3.58 eV, obtained by frequency doubling a cw Ti:sapphire laser in beta barium borate (BBO). Spectra were collected with 2 to 5 min integration times with a CCD after dispersion through a triple monochromator. Intensities of all spectra were corrected for instrument response using benzonitrile as an intensity and frequency reference [16]. RBM REPs [Fig. 1(b)] show clear $E_{33}$ and $E_{44}$ responses for (8,6), while the higher energy feature for (9,4) is not experimentally accessible. The single peak in the (10,5) REP further suggests the two transitions are closely spaced for this species. The $E_{ii}$ values obtained from the RBM REPs are a close match to the absorbance maxima. The REPs are fit using Eq. (1), in which Raman intensity ($I_{RRS}$) depends on excitation, transition, and phonon energies ($E_{L}$, $E_{ii}$, $E_{ph}$, respectively) and a damping term $\Gamma$. Because the relative signs of contributions from $E_{33}$ and $E_{44}$ can differ in Eq. (1), summing all terms before squaring can result in constructive or destructive combination to introduce quantum interference. Conversely, non-interacting states may be represented in Eq. (1) by instead first squaring the bracketed terms for each $E_{ii}$, then summing. $A$ and $B$ represent the square of the absorbance matrix elements for the two transitions. The exciton-phonon coupling matrix elements for resonance with incident and scattered photons (so-called ingoing and outgoing resonances), respectively, are $M_{1i}$ and $M_{2i}$. The relation $M_{2}/M_{1} = -(1 - C)/(1 + C)$ is used to introduce non-Condon effects, where $C$ gives the relative strength of non-Condon contributions [16]. We note in the absence of non-Condon effects ($C = 0$) that $M_{1i} = -M_{2i}$ [16]. For the fits in Fig. 1(b), $E_{ph}$ is fixed to the observed RBM frequency, while the other parameters are adjustable [19].

$$I_{RRS} \propto \left| A \left[ \frac{M_{13}^{33}}{E_{L} - E_{33} - i \frac{\Gamma_{33}^{13}}{2}} + \frac{M_{23}^{33}}{E_{L} - E_{33} - E_{ph} - i \frac{\Gamma_{33}^{23}}{2}} \right] + B \left[ \frac{M_{14}^{44}}{E_{L} - E_{44} - i \frac{\Gamma_{44}^{14}}{2}} + \frac{M_{24}^{44}}{E_{L} - E_{44} - E_{ph} - i \frac{\Gamma_{44}^{24}}{2}} \right] \right|^2$$

(1)

**FIG. 1 (color).** (a) Absorbance spectra of second, third, and fourth exciton transitions for (8,6) (red, $E_{33} = 3.31$ eV, $E_{44} = 3.50$ eV), (9,4) (blue, $E_{44} = 3.42$ eV, $E_{33} = 3.62$ eV), and (10,5) (green, $E_{33-44} = 3.22$ eV) SWCNT structures. (b) RBM REPs of third and fourth exciton transitions for (8,6) (red triangles), (9,4) (blue circles), and (10,5) (green squares) structures. Symbols: experimental data. Solid line: fit to data using Eq. (1) [19], with resulting $E_{ii}$ of 3.30 and 3.49 eV [$E_{33}$ and $E_{44}$ for (8,6)], 3.39 eV [$E_{44}$ for (9,4)], and 3.21 eV [$E_{33}$ and $E_{44}$ for (10,5)].

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We find the contrasting interference behaviors can also lead to anomalous LO/TO intensity ratios, depending on where in the REP one excites. Examples of (8,6) $G$-band spectra obtained at different excitation energies are shown in Figs. 3(a)–3(c). The different exciton-phonon coupling behavior discussed above for the LO and TO leads to REPs that are effectively out of phase with each other [Figs. 2(a) and 2(b)]. The result is that, while high energy excitations [Fig. 3(c)] are found to give the typically expected $G$-band spectrum (TO intensity $\ll$ LO), some excitations can lead to equal intensities [Fig. 3(a)]. Even more striking are the anomalous LO/TO ratios found for the (10,5) structure. Over nearly the entire excitation range [Figs. 3(d)–3(f) and Fig. 4(a)] TO intensities are found to be significantly stronger than or equal to those of the LO mode.

REPs for the (10,5) LO and TO modes at the overlapping $E_{33}$ and $E_{44}$ resonances are shown in Figs. 4(b) and 4(c), respectively. The LO REP differs significantly from those for the (8,6) and (9,4) structures, showing a weak and nearly featureless profile over most of the excitation range.

Furthermore, the non-Condon parameters that we extract ($C \sim 0.1$–0.5) are in agreement with values found previously for $E_{22}$ excitation [16].

FIG. 2 (color). (a) and (b) (8,6) $G$ and $G$ REP energies, respectively. (c) and (d) (9,4) $G$ and $G$ REPs, respectively. Symbols: experimental data. Red dotted line: model excluding interference and non-Condon effects. Magenta dashed line: fit including interference effects and non-Condon effects [19]. Solid vertical lines designate $E_{33}$ positions (ingoing resonances), while vertical dashed lines designate positions of $E_{44}$ + phonon energies (outgoing resonances). (e) Depiction of how relative sign of exciton-phonon coupling elements changes for $G$ vs $G$ on going from $E_{33}$ to $E_{44}$ excitation. Horizontal position of signs represents relative alignment of relevant ingoing and outgoing resonances.

modeling for three limiting cases overlaid on the experimental data. Inspection of Fig. 2 for the first case shows that an assumption of noninteracting states with no non-Condon effects ($C = 0$) qualitatively represents the LO mode behavior for both chiralities. However, it gives a poor quantitative fit and is unable to describe the more complex behavior of the TO mode [Figs. 2(b) and 2(d)]. Significant improvement is found in the second case for both the LO and TO modes, in which the $E_{33}$ and $E_{44}$ Raman responses are allowed to interfere. Finally, when both quantum interference and non-Condon effects are included, excellent quantitative agreement between the fits and data is found for both modes in both chiralities.

Most importantly, the observed interference provides insight into how the exciton-phonon coupling processes change with $E_{ii}$. First, we note that, as seen in the modeling results [red dotted line, Fig. 2(a)–2(d)] and as confirmed experimentally (see Ref. [16]), in the absence of quantum interference the REP shapes for the LO and TO are expected to behave similarly across their resonance windows. Instead, we observe here very different intensity profiles on comparing the LO to TO behaviors. In the vicinity of where the outgoing resonance of the lower energy transition overlaps with the ingoing resonance of the higher state [at $\sim 3.49$ eV for (8,6) and $\sim 3.58$ eV for (9,4)] the LO mode shows a significant enhancement of intensity, while the TO is suppressed. This opposing behavior of the two modes is a clear signature of interference and arises as a consequence of the opposite way in which the signs of the exciton-phonon coupling matrix elements for the two modes vary on going from $E_{33}$ to $E_{44}$. Good fits to the data can only be obtained if the relative signs of ingoing and outgoing resonances ($M_1$ and $M_2$, respectively) for the LO mode are reversed between $E_{33}$ and $E_{44}$. In contrast, they remain the same for the TO mode. These sign behaviors are depicted in Fig. 2(e). Because the $E_{33}$ and $E_{44}$ energy spacing is approximately equal to the $G$-phonon energy, the result is constructive interference for the LO mode and destructive interference in the TO mode. We note that this contrasting behavior in the matrix elements has been predicted previously [20,21]. It is only the significant quantum interference present in the (8,6) and (9,4) structures that has allowed us to reveal experimentally this aspect of exciton-phonon coupling here.

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and sits on a nonzero continuum background. Similar to the (8,6) and (9,4), however, the (10,5) TO REP shows an initial peak that drops to a lower intensity shoulder at higher energies.

Both the LO and TO REP features can be understood and modeled by applying the principles extracted from the (8,6) and (9,4) fits. One further consideration must be taken. As noted in the data of Fig. 1, the occurrence of a single spectral feature in both the absorbance spectrum and the RBM REP for the (10,5) suggests that its $E_{33}$ and $E_{44}$ transitions are nearly equal in energy. Given $\Gamma$ values of $\sim 120$ meV, the two transitions would be visually resolved in the RBM REP at energy separations ($\Delta E_{33-44}$) of 50 meV or greater. Thus, $\Delta E_{33-44}$ must be less than 50 meV. To test these principles, we first simulated LO and TO REPs using the relative behavior of the matrix elements from Fig. 2(e), applying a $C = 0.2$, while varying $\Delta E_{33-44}$. Within these constraints, when $\Delta E_{33-44}$ is about one $G$ phonon of energy, the (8,6) and (9,4) REP features are recovered [19]. However, the main features of the (10,5) REPs cannot be reproduced unless $\Delta E_{33-44}$ is brought to 10 meV or less [19], further suggesting their energy separation must be small.

Applying these principles to fitting of the (10,5) REPs [using $E_{ii}$ and $\Gamma$ values extracted from the (10,5) absorbance and RBM data as starting points] results in excellent fits to the data. For the LO mode [Fig. 4(b)], a $\Delta E_{33-44}$ of $\sim 1$ meV [19] leads to nearly complete destructive interference, explaining the weak and featureless REP. That any LO intensity remains is likely due to differences in the magnitude of the $E_{33}$ and $E_{44}$ matrix elements. Non-Condor effects must also be included. However, while $C \sim 0.2$ is necessary to reproduce the data, its value is poorly constrained. We note the weak LO intensity also makes apparent a background contribution that may arise as a combination of nonresonant response plus contributions from overlapping $E_{ii}$ continuum states [22]. We model these contributions by incorporating into Eq. (1) a constant term ($Ve^{i\theta}$, with $V = -0.19$ and $\theta = 0.066$) [19]. Solid vertical line designates $E_{33,44}$ position (ingoing resonance), while vertical dashed line designates position of $E_{33,44} + \text{phonon energy (outgoing resonance)}$.

The excellent fitting of the TO REP [Fig. 4(c)] also gives a $\Delta E_{33-44}$ of $\sim 1$–2 meV, consistent with the LO result. This condition results in strong constructive interference for the TO mode. The anomalous (10,5) LO/TO ratios shown in Figs. 3(d)–3(f) are thus understood as a result of the strongly opposing interference effects acting on the two modes. Because $\Delta E_{33-44}$ approaches zero, the asymmetry observed for the (10,5) TO REP is solely determined...
by non-Condon effects, allowing an accurate determination of $C = 0.22 \pm 0.02$.

While extended tight binding calculations [18] predict a small $(10,5) \Delta E_{33-44} \approx 50 \text{ meV}$, the nearly 0 meV energy separation demonstrated here is a remarkable result. Whether this is a simple accident of electronic structure acted on by trigonal warping [15] or arises from additional unrecognized perturbations remains an open question for further study. Furthermore, with states so close in energy there may be unanticipated consequences for relaxation processes and pathways from excitations into this region for $(10,5)$, providing motivation for performing dynamics measurements on this specific tube structure following excitation into $E_{33}$ and $E_{44}$. Theoretical studies aimed at exploration of the possible consequences for other photophysical responses will also be of interest in this regard. The REP data also represent an ideal test system for modeling Raman response based on theoretical determination of the matrix elements for absorption [$A$ and $B$, Eq. (1)] and exciton-phonon coupling ($M_{ij}$), $\Gamma$, and the recently revealed non-Condon effects ($C$) [16]. Additionally, the possibility of pairing the REPs with single-chirality absorption spectra makes the data well suited for modeling via Raman transform analysis [23,24] as an alternate to the sum-over-states approach used here [Eq. (1)].

In summary, through a judicious choice of specific chiral structures we have demonstrated unambiguously quantum interference effects in the Raman response from resonance excitation of closely spaced $E_{33}$ and $E_{44}$ transitions in mod 2 semiconducting SWCNTs. Such a clear demonstration results from a direct comparison of the global behaviors of the LO and TO modes across multiple tube structures. Observation of constructive and destructive interference effects are described self-consistently for each mode at the different energy spacings available with each structure. This ability allows extraction of the relative behavior of the signs of the Raman matrix elements, which can be important in determining a wide range of nonlinear optical responses and provides additional insight into the exciton-phonon coupling processes that underlie a tremendous range of nanotube photophysical behaviors. Additionally, our demonstration of quantum interference as the source of anomalous LO/TO intensity ratios may provide a mechanism for similarly observed behaviors commonly seen in single-tube Raman spectroscopy. Finally, our results demonstrate that non-Condon effects, only recently found to be important in the $G$-band Raman response in $E_{22}$ excitation [16], must also be considered for the higher lying exciton transitions. These results also emphasize the importance of the availability of pure chirality samples for enabling the study of previously inaccessible optical behaviors in carbon nanotubes.

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[19] See Supplemental Material at http://link.aps.org/supplemental/10.1103/PhysRevLett.108.117404 for all G-band spectra used in generating REPs, REP simulations as a function of $\Delta E_{ij}$, a discussion of the sensitivity of the $(10,5)$ fits to $\Delta E_{ij}$, additional discussion of how continuum contributions are included in the $(10,5)$ fitting, and tabulation of REP fitting parameters.


